

Exercises

3.290 [065] Prerequisites: [064], [01G]. Given sets $A_1, A_2 \dots$ and $B_1, B_2 \dots$, for $n \in \mathbb{N}$, say if there is a relation (of equality or containment) between

$$\left(\liminf_{n \rightarrow \infty} A_n\right) \cap \left(\liminf_{n \rightarrow \infty} B_n\right) \stackrel{?}{=} \liminf_{n \rightarrow \infty} (A_n \cap B_n) \quad (3.290)$$

$$\left(\liminf_{n \rightarrow \infty} A_n\right) \cup \left(\liminf_{n \rightarrow \infty} B_n\right) \stackrel{?}{=} \liminf_{n \rightarrow \infty} (A_n \cup B_n) \quad (3.291)$$

If equality does not hold, show an example. Then use [063] to establish similar rules for $\limsup_{n \rightarrow \infty} A_n$.

Solution 1. [066]