**Definition 3.95.** [OBN] A directed set is an ordered set 
$$(X, \leq)$$
 for which  $\forall x, y \in X \ \exists z \in X, \ x \leq z \land y \leq z$  . (3.96)