Definition 3.219. [ort] A nonempty subset $S \subseteq X$ is an **initial segment** if $\forall x \in S, \forall y \in X, \ y < x \Rightarrow y \in S$.