Exercises

3.143 [091] Let D, C be non-empty sets and $f : D \to C$ a function. Let I a non-empty family of indexes, $B_i \subseteq C$ for $i \in I$. Given $B \subseteq C$ remember that the **counterimage** of B is

$$f^{-1}(B) \stackrel{\text{\tiny def}}{=} \{ x \in D, f(x) \in B \} ,$$

Given $B \subseteq C$ we write $B^c = \{x \in C, x \notin B\}$ to denote the complement. Show these counterimage properties.

$$f^{-1}(\bigcup_{i \in I} B_i) = \bigcup_{i \in I} f^{-1}(B_i)$$
(3.143)
$$f^{-1}(\bigcap_{i \in I} B_i) = \bigcap_{i \in I} f^{-1}(B_i)$$
(3.144)
$$f^{-1}(B^c) = f^{-1}(B)^c .$$
(3.145)