E7.31 [OFO] Note: Exam of 9th APr 2011. Let  $(a_n)$  be a sequence of real numbers (not necessarily positive) such that the series  $\sum_{n=1}^{\infty} a_n$  converges

to  $a \in \mathbb{R}$ ; let  $b_n = \frac{a_1 + \dots + a_n}{n}$ ; show that if the series  $\sum_{n=1}^{\infty} b_n$ 

converges then a = 0.

Exercises