E8.85 [OKX] Let \mathcal{B} be a base for a topology τ on X; then the following two properties apply.

(a)
$$\bigcup \mathcal{B} = X$$
 that is, the union of all the elements of the base is X .

Exercises

Solution 1. [OKY]

(b) Given $B_1, B_2 \in \mathcal{B}$ for each $x \in B_1 \cap B_2$ there exists $B_3 \in \mathcal{B}$

such that $x \in B_3 \subseteq B_1 \cap B_2$.