E9.4 [OMX] We generalize the definition of *metric space* assuming that d: $X \to [0, \infty]$ (the other axioms are the same). Show that the relation

Exercises

Solution 1. **FOMY**7

 $x \sim v$ defined by

$$x \sim y \iff d(x,y) < \infty$$
 is an equivalence relation, and that equivalence classes are open

is an equivalence relation, and that equivalence classes are open, and therefore are disconnected from each other.