

Definition 11.23. [110] If M_1, M_2 are vector spaces with norms $\|\cdot\|_{M_1}$ and respectively $\|\cdot\|_{M_2}$, then φ is an isometry when

$$\forall x, y \in M_1, \|x - y\|_{M_1} = \|\varphi(x) - \varphi(y)\|_{M_2} \quad (11.24)$$

(rewriting the definition of distance using norms).