Definition 14.4. [16x] Let $C \subseteq \mathbb{R}^n$ be a set; it is called convex if

$$\forall t \in [0,1], \ \forall x, y \in C, \ (tx + (1-t)y) \in C$$

that is, if the segment connecting each $x, y \in C$ is all inclusive in C.