

Exercises

E15.c.2 [18F] Show that $f(x)$ is convex if and only if the map $R(x, y) = \frac{f(x)-f(y)}{x-y}$ is monotonically weakly increasing in x .^a Moreover, f is strictly convex if and only if R is strictly increasing.

Solution 1. [18G]

^aNote that $R(x, y)$ is symmetrical.