

Exercises

14.31 [18K] Prove that a continuous function $f : (a, b) \rightarrow \mathbb{R}$ is convex if and only if, for every $u, v \in (a, b)$,

$$f\left(\frac{u+v}{2}\right) \leq \frac{f(u) + f(v)}{2} .$$