Exercises

E15.2 [1BW] Let $f : [a, b] \to \mathbb{R}$ continuous and such that

$$\int_a^b f(x)g(x) \, \mathrm{d}x = 0$$

for any $g : [a, b] \to \mathbb{R}$ continuous: prove that $f \equiv 0$.