**Definition 21.2.** [1NV] Let  $I \subseteq \mathbb{R}$  be an interval.

- A continuous function γ : I → X is called parametric curve, or more simply in the following curve.
- If  $\gamma$  is injective, the curve is said to be **simple**.
- If  $\gamma$  is a homeomorphism onto its image, the curve is said to be **embedded**.
- If  $X = \mathbb{R}^n$  and  $\gamma$  is of class  $C^1$  and  $\gamma'(t) \neq 0$  for every  $t \in I$ , then  $\gamma$  is called an **immersed curve** or **regular curve**.

We will call **support** or **trace** the image  $\gamma(I)$  of a curve. The term arc is also used as a synonym for curve; <sup>a</sup> this term is mainly used when the curve is not (necessarily) closed.

<sup>&</sup>lt;sup>*a*</sup>Note that in the book [26] an *arc* is an injective curve.