

**Remark 3.14.** *[1X1] (Solved on 2022-10-11) The variable  $x$ , which is quantified in a part of a formula, is again free if it is reused in another piece of the formula; this is syntactically permissible but makes the formula less readable, as in this example that uses the language of set theory*

$$A \subseteq \mathbb{N} \wedge x \in \mathbb{N} \wedge x \geq 4 \wedge (\forall x \in A, x \leq 10)$$

*which should be written as*

$$A \subseteq \mathbb{N} \wedge x \in \mathbb{N} \wedge x \geq 4 \wedge (\forall y \in A, y \leq 10)$$

*renaming the variable inside the part where it is quantified.*