

Exercise 5.8. [1ZY] Not all fields are infinite sets. Consider $X = \{0, 1\}$ and operations $0+0 = 1+1 = 0$, $0+1 = 1+0 = 1$, $0 \cdot 0 = 0 \cdot 1 = 1 \cdot 0 = 0$ and $1 \cdot 1 = 1$. Check that it is a field. Show that it cannot be an ordered field.