

Exercise 5.8. [1zz] Consider the ring of matrixes $\mathbb{R}^{2 \times 2}$ let's define

$$A = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} , \quad B = \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix} ,$$

then check that

$$AB = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix} , \quad BA = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} ;$$

you conclude that the ring of matrixes is not commutative.