**Exercise 5.8.** [200] Let's fix an integer N > 2 that it is not a perfect square. Consider the subset F of  $\mathbb R$  given by the numbers x that can be written as  $x = a + b\sqrt{N}$ , with  $a, b \in \mathbb{Q}$ ; we associate the operations of  $\mathbb{R}$ : show that *F* is a field.

## Solution 1. [201]