**Exercise 7.31.** [210] Note:exercise 2, written exam 15 January 2014. Let  $(a_n)_{n\geq 0}$  be a sequence of positive real numbers. Having defined  $s_n = \sum_{i=0}^n a_i$  prove that:

• the series  $\sum_{n=0}^{\infty} a_n$  converges if and only if the series  $\sum_{n=0}^{\infty} a_n/s_n$  converges;

• the series 
$$\sum_{n=0}^{\infty} a_n / (s_n)^2$$
 converges.

## Solution 1. [21K]