**Definition 3.141.** [22R] Let  $A \subseteq X$ . The majorants of A (or upper bounds) are

$$M_A \stackrel{\text{\tiny def}}{=} \{ x \in X : \forall a \in A, a \le x \} \quad .$$

A set A is **bounded above** when there exists an  $x \in X$  such that  $\forall a \in A, a \leq x$ , i.e. exactly when  $M_A \neq \emptyset$ .

If  $M_A$  has minimum s, then s is th **supremum**, a.k.a. **least upper bound**, of A, and we write  $s = \sup A$ .

By reversing the order relation in the above definition, we obtain the definition of **minorants/lower bounds, bounded below, infimum/greatest** lower bound.