

Definition 3.70. [23X] A relation R between elements of A is said to be:

- **reflexive** if xRx for any $x \in A$;
- **irreflexive** or **anti-reflexive** if $\neg xRx$ for any $x \in A$;
- **symmetric** if xRy implies yRx for any $x, y \in A$;
- **antisymmetric** if aRb and bRa imply $a = b$, for any $a, b \in A$;
- **trichotomous** if for all $x, y \in A$ one and exactly one of xRy , yRx and $x = y$ holds;
- **transitive** if xRy and yRz imply xRz , for any $x, y, z \in A$.

A relation R between elements of A and elements of B is said to be:

- **injective** (also called left-unique) if xRy and zRy imply $x = z$, for any $x, z \in A, y \in B$;
- **functional** (also called right-unique) if xRy and xRz imply $y = z$, for any $x \in A, y, z \in B$; such a binary relation is called a “partial function” (see also [1YR], [01P]);
- **total** (also called “left-total”) if for any $x \in A$ there is a $y \in B$ such that xRy ;
- **surjective** (also called “right-total”) if for any $y \in B$ there is a $x \in A$ such that xRy .