

Proposition 4.39. *[28B] \leq is an order relation.*

Proof. Reflexive property: $n+0 = n$. Antisymmetric property: if $n+k = m$ and $m+h = n$ then $n+k+h = n$ therefore by cancellazione [27V] $h+k = 0$, and for [27W] $h = k = 0$ so $n = m$. Transitive property: if $n+k = m$ and $m+h = p$ then $n+k+h = p$. \square