

6.5 Upper and lower limits

[29P]

From the previous definition we move on to the definitions of “*limit superior*” \limsup and “*limit inferior*” \liminf . The idea is so expressed.

Definition 6.37. [20F]

Remark 6.38. [20G]

In particular, defining $l = \limsup_{x \rightarrow x_0} f(x)$, the previous formulas characterize exactly the “limsup”.

Corollary 6.39. [20N]

We make them explicit further in what follows. (It is recommended to try to rewrite autonomously some items, by way of exercise).

Proposition 6.40. [0BK]

Remark 6.41. [0BM]

Remark 6.42. [0BN]

Exercises

E6.43 [0BP]

E6.44 [0BQ]

E6.45 [29R]

E6.46 [29S]

E6.47 [29T]

Other exercises on limits of sequences can be found in Sec. [0CN].