

Definition 17.2. [2DT] Consider a set A , a function $f : A \rightarrow \mathbb{R}$ and a sequence of functions $f_n : A \rightarrow \mathbb{R}$. We will say that f_n converges to f pointwise if

$$\forall x \in A, \lim_{n \rightarrow \infty} f_n(x) = f(x) \quad .$$

We will say that f_n converges to f uniformly if

$$\forall \varepsilon > 0 \exists N \in \mathbb{N}, \forall n \geq N, \forall x \in A, |f_n(x) - f(x)| < \varepsilon \quad .$$